# **St. Peter the Apostle High School**

# **Mathematics Dept.**



# PracticePrelim TwoPaper 2

## **Duration: 1 Hr 30 Mins**

Marks: 50

- 1. Attempt ALL questions.
- 2. You <u>MAY</u> use a calculator.
- **3.** Write your solutions on the blank paper provided.
- 4. Full credit will be given only where the solution contains appropriate working.
- 5. Square-ruled paper will be provided if necessary.

### **Formula Sheet**

The roots of 
$$ax^2 + bx + c = 0$$
 are  $x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$ 

Sine rule:

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Cosine rule:

$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$
 or  $\cos A = \frac{b}{c}$ 

$$=\frac{b^2+c^2-a^2}{2bc}$$

Area of a triangle: Area =  $\frac{1}{2}ab \sin C$ 

Volume of a sphere: Volume =  $\frac{4}{3}\pi r^3$ 

Volume of a cone: Volume =  $\frac{1}{3}\pi r^2 h$ 

Volume of a pyramid: Volume = 
$$\frac{1}{3}Ah$$

Standard deviation: 
$$s = \sqrt{\frac{\sum (x - \overline{x})^2}{n-1}} = \sqrt{\frac{\sum x^2 - (\sum x)^2 / n}{n-1}}$$
, where n is the sample size.

1.	A painting was valued at £40 000 in 2012. The owner plans to sell it in 2015 and hopes that it will be worth at least £50 000.	<u>Marks</u>
	If the painting increases in value at the rate of 8% per annum, will it be worth at least £50 000 in 2015?	
	You must show all your working and give a reason for your answer.	3
2.	Write as a single fraction in its simplest form: $\frac{4b}{7x} \div \frac{b}{x^3}$	3
3.	A conical container has a capacity of 5 litres and height 18 cm. Calculate its radius.	3
4.	Find the point of intersection of the lines which have equations: $3x - 4y = 17$ $5x - 2y = 19$	3
5.	<ul> <li>a) The number of calls made to a call centre in week 1 were as follows:</li> <li>59 44 55 56 46 50 54</li> <li>Calculate the mean and standard deviation for week 1.</li> </ul>	3
	b) In week 2 the number of calls received at the call centre gave a mean of 75 and a standard deviation of 4.6.	
	Make two comparisons between the number of calls received at the call centre during week 1 compared to week 2.	2

The diagram below shows a square based pyramid PQRST. 6. P h R

Q g S. T f

Express  $\overrightarrow{RP}$  in terms of  $\underline{f}$ ,  $\underline{g}$  and  $\underline{h}$ .

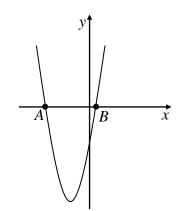
3

7. The graph in the diagram has equation

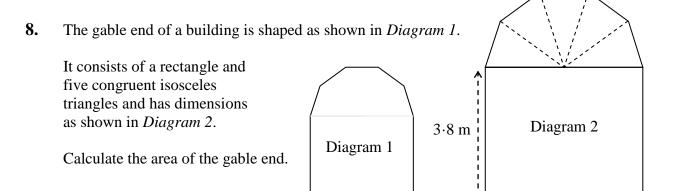
$$y = 3x^2 + 2x - 3$$

and cuts the *x*-axis at *A* and *B*.

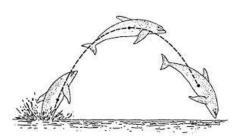
Find the coordinates of the points *A* and *B* giving your answers correct to 1 decimal place.



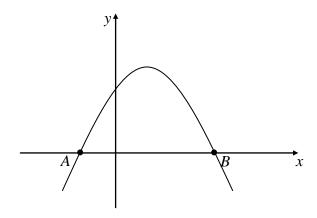
Marks



9. When a fish 'leaps' from the water its path is in the shape of a parabola.



The parabola can be represented by the equation  $y = 5 + 4x - x^2$ .



€-

4.6 m

This cartesian diagram shows the parabola.

- a) If one unit on the graph represents a distance of 20cm, calculate how far the fish travels horizontally during one 'leap'.
- b) Does the fish reach a height of 1.75 metres on this leap?You must show all your working to justify your answer.

3

4

#### <u>Marks</u>

4

4

**10.** The diagram below shows the cross section of a cylindrical tank with radius 18cm.

There is liquid in the tank and its surface, AB, measures 27cm.

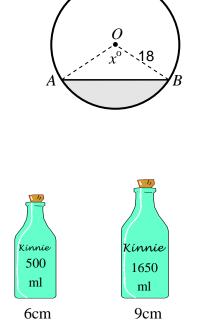
It is thought that angle *AOB* might be 90°.

Without using trigonometry, decide whether or not this is the case.

 The national soft drink of Malta is called "Kinnie" and it is sold in various bottle sizes. Two are shown here:

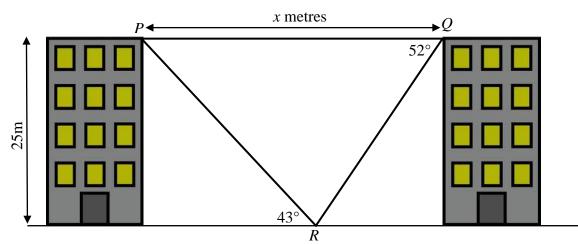
The smaller bottle has a base diameter of 6cm and holds 500ml.

The larger bottle has a base diameter of 9cm and it holds 1650ml.



The bottles look alike but could they actually be mathematically similar?

12. The diagram shows 2 blocks of flats of equal height, each 25m tall.



**P** and **Q** represent points on the top of the flats and **R** represents a point on the ground between them.

From **Q**, the angle of depression is  $52^{\circ}$ . From **R**, the angle of elevation to **P** is  $43^{\circ}$ .

Calculate the distance, *x* metres, between the 2 flats. Give your answer correct to 2 decimal places