

St. Peter the Apostle High School

Mathematics Dept.



Practice Prelim Five Paper 1

Duration: 1 Hour

Marks: 40

1. Attempt ALL questions.
2. You **MAY NOT** use a calculator.
3. Write your solutions on the blank paper provided.
4. Full credit will be given only where the solution contains appropriate working.
5. Square-ruled paper will be provided if necessary.

Formula Sheet

The roots of $ax^2 + bx + c = 0$ are $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Sine rule: $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine rule: $a^2 = b^2 + c^2 - 2bc \cos A$ or $\cos A = \frac{b^2 + c^2 - a^2}{2bc}$

Area of a triangle: $\text{Area} = \frac{1}{2} ab \sin C$

Volume of a sphere: $\text{Volume} = \frac{4}{3} \pi r^3$

Volume of a cone: $\text{Volume} = \frac{1}{3} \pi r^2 h$

Volume of a pyramid: $\text{Volume} = \frac{1}{3} Ah$

Standard deviation: $s = \sqrt{\frac{\sum (x - \bar{x})^2}{n - 1}} = \sqrt{\frac{\sum x^2 - (\sum x)^2 / n}{n - 1}}$, where n is the sample size.

1. Calculate $2\frac{1}{6} \times \frac{2}{5}$ 2

2. Find the gradient and y-intercept of the line with equation $5x + 7y + 35 = 0$ 3

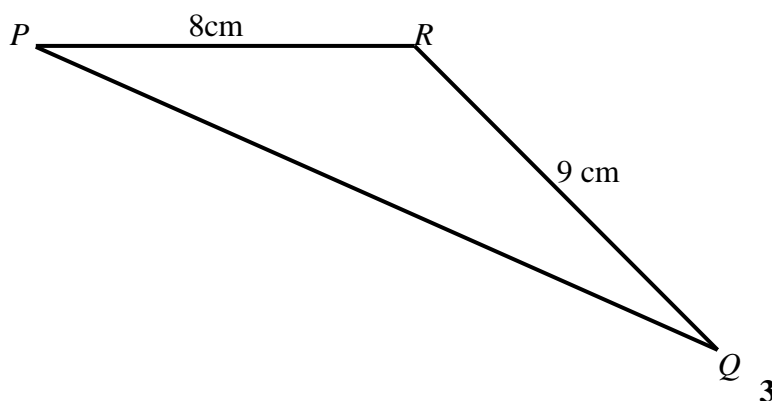
3. Change the subject of this formula $V = \pi r^2 h$ to 'r' 2

4. a) Factorise: $25x^2 - 49$ 2
- b) Factorise fully: $10x^2 + 9x - 7$ 2
- c) Hence, or otherwise, simplify $\frac{25x^2 - 49}{10x^2 + 9x - 7}$ 1

5. Vectors \underline{a} and \underline{b} have components as follows: $\underline{a} = \begin{pmatrix} 4 \\ -3 \\ 4 \end{pmatrix}$ and $\underline{b} = \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix}$
- a) Find the components of the vector represented by $\underline{a} - 2\underline{b}$ 1
- b) Calculate the magnitude of the vector represented by $\underline{a} - 2\underline{b}$ 2

6. Multiply the brackets and simplify: $(x - 2)(5x^2 - 4x - 2)$ 3

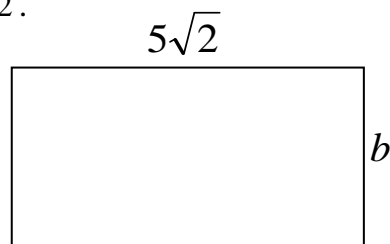
7. For the triangle PQR calculate the **exact value** of $\sin RPQ$ if:
the exact value of $\sin PQR$ is $\frac{1}{3}$
 $AC = 8\text{cm}$ and $BC = 9\text{cm}$



8. The area of this rectangle is 24 cm^2 . It has length $5\sqrt{2}$.

Calculate its breadth, b , leaving your answer as a surd in its simplest form with a rational denominator.

Dimensions are in centimetres.



3

9. Write as a single fraction in its simplest terms $\frac{2}{x-2} - \frac{5}{x+1}$, $x \neq 2$; $x \neq -1$

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10. Simplify $x^4 y^3 \div x^6 y$ expressing your answer with positive powers.

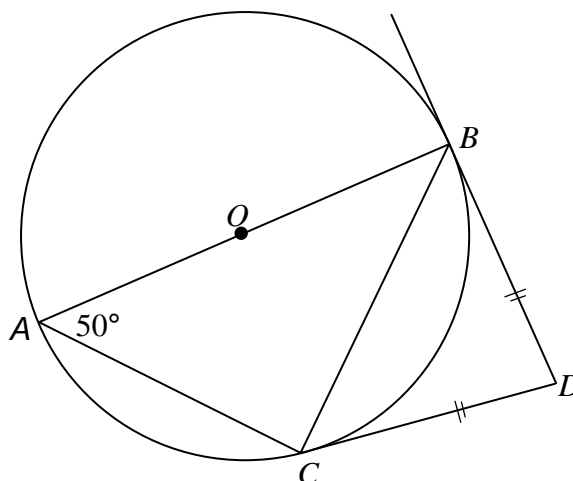
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11. AB is a diameter and O is the centre of the circle shown below.

BD is a tangent to the circle with B the point of contact.

Triangle BCD is isosceles.

Given that angle $BAC = 50^\circ$, find the size of angle BDC .



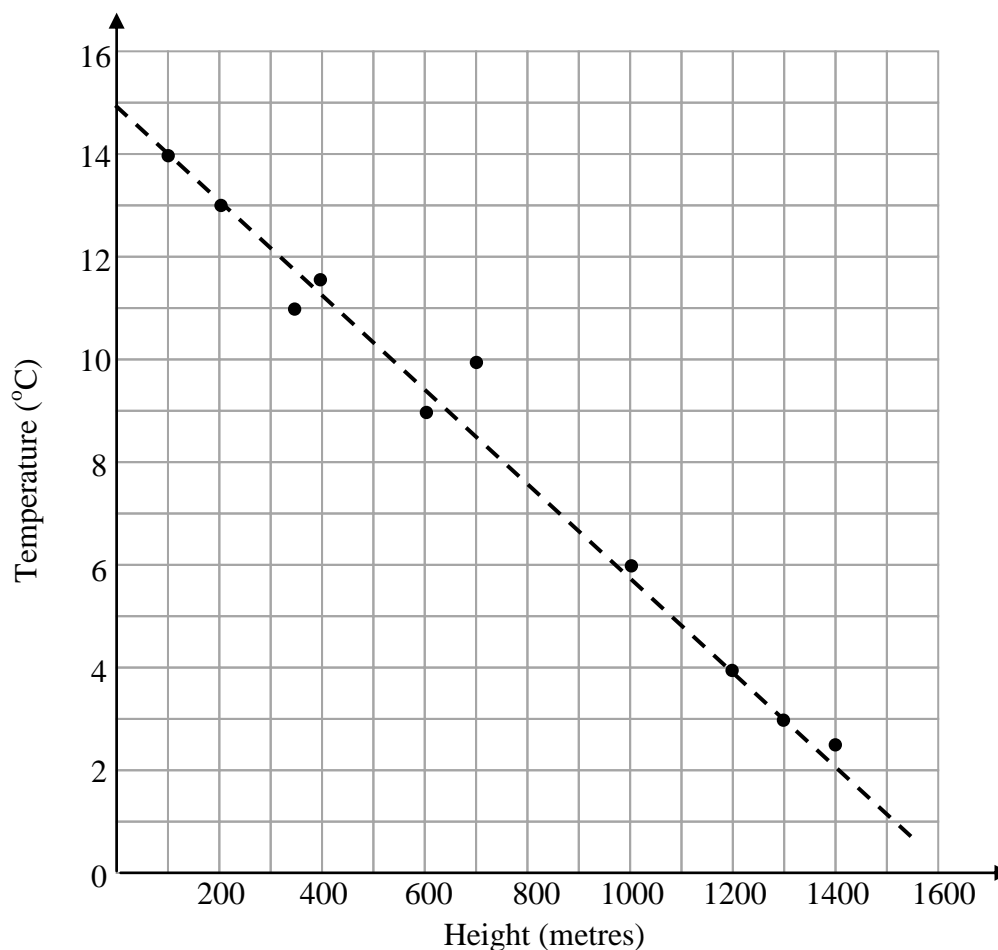
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12. The graph shows the height above sea level, in metres, of ten places in Scotland and the corresponding mean temperature in degrees Celsius.

St. Andrews in Fife is 100 m above sea level and has a mean temperature of 14°C

The top of the Caitngorm is 1300 m above sea level and has a mean temperature of 3°C

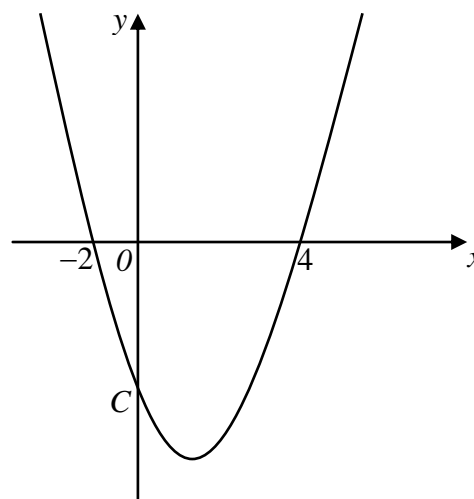
Determine the equation of the line of best fit which has also been drawn on the graph.



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13. The graph shown has equation $y = (x + 2)(x - 4)$.

- Find the coordinates of point C, where the graph cuts the y-axis.
- Find the coordinates of the turning point.
- State the equation of the axis of symmetry of the parabola.



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