

N5

Indices

Expressions & Formulae

SPTA Mathematics - Topic Questions with Notes



Rules of Indices

Basic Rule 1: anything to the power 0 is equal to 1:

$$\text{e.g. } 5^0 = 1, \quad 17^0 = 1, \quad 35627658^0 = 1, \quad x^0 = 1$$

Basic Rule 2: anything to the power 1 is equal to itself:

$$\text{e.g. } 5^1 = 5, \quad 17^1 = 17, \quad 35627658^1 = 35627658, \quad x^1 = x$$

Key Rule 1: when you multiply two expressions involving powers, you add the numbers in the power: $a^m \times a^n = a^{m+n}$

$$\text{e.g. } x^3 \times x^4 = \underline{x^7} \quad y^{-1} \times y^6 = y^{-1+6} = \underline{y^5}$$

Key Rule 2: when you divide two expressions involving powers, you take away the numbers in the power: $\frac{a^m}{a^n} = a^{m-n}$

$$\text{e.g. } a^8 \div a^3 = \underline{a^5} \quad \frac{m^{10}}{m^8} = \underline{m^2}$$

Key Rule 3: when you take one power to the power of another (nested powers), you multiply the numbers in the power: $(a^m)^n = a^{mn}$

$$\text{e.g. } (x^2)^3 = \underline{x^6} \quad (a^4)^{-2} = \underline{a^{-8}}$$

Example 1

Simplify $\frac{3x^4 \times 8x^8}{6x^2}$

Solution

$$\begin{aligned} \frac{3x^4 \times 8x^8}{6x^2} &= \frac{24x^{12}}{6x^2} && \text{(add the powers when multiplying)} \\ &= 4x^{10} && \text{(take away the powers when dividing)} \end{aligned}$$

Example 2

Simplify $(5x^{-3})^2 \times x^8$

Solution

$$\begin{aligned}(5x^{-3})^2 \times x^8 &= 25x^{-6} \times x^8 && \text{(multiplying the nested powers)} \\ &= 25x^2 && \text{(adding the powers when multiplying)}\end{aligned}$$

Example 3

Simplify $3x^2(x^{-2} + 2x^5)$

Solution

$$\begin{aligned}3x^2(x^{-2} + 2x^5) &= 3x^2 \times x^{-2} + 3x^2 \times 2x^5 \\ &= 3x^{2+(-2)} + 6x^{2+5} \\ &= 3x^0 + 6x^7 \\ &= \underline{\underline{3 + 6x^7}}\end{aligned}$$

Exercise 1

1. Write each of the following in its simplest index form.

a) $3^4 \times 3^2$	b) 2×2^3	c) $10^5 \times 10^2$	d) $8^3 \times 8^5$
e) $7^6 \times 7$	f) $5^4 \times 5^4$	g) $9^6 \times 9^2$	h) $6^8 \times 6^5$
i) $x^3 \times x^5$	j) $c^2 \times c^9$	k) $a^2 \times a^{12}$	l) $y^5 \times y^5$
m) $b^{10} \times b^{30}$	n) $p \times p^9$	o) $d^2 \times d^4$	p) $q^{11} \times q^9$
q) $t^3 \times t^7$	r) $f^4 \times f^3$	s) $k \times k^{12}$	t) $z^{50} \times z^{50}$
u) $x^{30} \times x^{50}$	v) $y^{19} \times y$	w) $a^{25} \times a^{65}$	x) $b^1 \times b^0$

2. Write each of the following in its simplest index form.

a) $2^8 \div 2^3$	b) $5^4 \div 5^2$	c) $12^9 \div 12^6$	d) $7^{11} \div 7^4$
e) $20^5 \div 20$	f) $8^8 \div 8^4$	g) $3^{18} \div 3^3$	h) $4^{15} \div 4^{13}$
i) $x^7 \div x^2$	j) $a^9 \div a^5$	k) $y^{20} \div y^{10}$	l) $b^4 \div b^1$
m) $p^{12} \div p^{11}$	n) $c^7 \div c^7$	o) $q^8 \div q^2$	p) $d^4 \div d$
q) $\frac{x^9}{x^3}$	r) $\frac{a^8}{a^2}$	s) $\frac{m^{14}}{m}$	t) $\frac{s^7}{s^7}$
u) $\frac{d^{20}}{d^{12}}$	v) $\frac{y^{100}}{y^{10}}$	w) $\frac{t^{100}}{t}$	x) $\frac{w^{10}}{w^0}$

3. Write each of the following in its simplest index form.

- | | | | |
|---------------------|----------------------|-------------------------|----------------------|
| a) $(3^2)^4$ | (b) $(8^2)^2$ | (c) $(10^3)^2$ | (d) $(2^2)^5$ |
| e) $(4^5)^3$ | (f) $(1^7)^2$ | (g) $(12^3)^3$ | (h) $(5^5)^5$ |
| i) $(x^4)^2$ | (j) $(y^8)^5$ | (k) $(a^3)^7$ | (l) $(m^4)^4$ |
| m) $(b^3)^6$ | (n) $(p^5)^3$ | (o) $(k^5)^{20}$ | (p) $(z^6)^0$ |

4. Write the following without brackets.

- | | | | |
|-----------------------|-----------------------|-------------------------|------------------------|
| a) $(2b)^2$ | (b) $(7a)^3$ | (c) $(3x)^4$ | (d) $(2y)^5$ |
| e) $(ab)^4$ | (f) $(xy)^7$ | (g) $(wz)^5$ | (h) $(st)^3$ |
| i) $(pq^2)^3$ | (j) $(x^4y)^2$ | (k) $(a^2b^3)^5$ | (l) $(6a^5)^2$ |
| m) $(10x^2)^3$ | (n) $(2c^4)^5$ | (o) $(3ab^2)^3$ | (p) $(4m^2k)^2$ |

5. Simplify these expressions.

- | | | | |
|--|--|--|---|
| a) $2a^3 \times 5a^5$ | (b) $7x \times 9x^8$ | (c) $12p^7 \div 4p^4$ | (d) $50b^{12} \div 10b^6$ |
| e) $3y \times (2y^2)^3$ | (f) $(4q^3)^2 \times 5q^4$ | (g) $(4c^3)^3 \div 8c^2$ | (h) $72z^{12} \div (3z^4)^2$ |
| i) $k^2(k^3 + k^5)$ | (j) $m^5(m^2 - m^3)$ | (k) $2x^4(x^3 + 3x^2)$ | (l) $5a^5(2a^2 - 3a^3)$ |
| m) $\frac{x^5 \times x^4}{x^6}$ | (n) $\frac{(m^5)^4}{m^6}$ | (o) $\frac{5c^3 \times 4c^7}{2c^6}$ | (p) $\frac{(3q^3)^2 \times 4q^4}{6q^7}$ |
| q) $\frac{(3xy^5)^3}{9x^2y}$ | (r) $\frac{(2a^2b^5)^6}{(4ab)^2}$ | (s) $\frac{(4p^4)^3}{2p^3 \times 8p^6}$ | (t) $\frac{(2ab^3)^5}{3a^2b \times 4ab^2}$ |

6. Write down the value of

- | | | | |
|--------------------|----------------------------|-----------------------|---------------------------|
| a) 5^0 | (b) 2^0 | (c) 100^0 | (d) $(-3)^0$ |
| e) 25^0 | (f) $\frac{1}{2}^0$ | (g) a^0 | (h) k^0 |
| i) $(mn)^0$ | (j) $(ab^2)^0$ | k) $(10x^3)^0$ | (l) $(16y^2z^3)^0$ |

Negative Powers and Fractions in Powers

A negative power means dividing. In general, $a^{-m} = \frac{1}{a^m}$

$$\text{e.g. } 3^{-2} = \frac{1}{3^2} = \frac{1}{\underline{\underline{9}}}$$

$$a^{-4} = \frac{1}{\underline{\underline{a^4}}}$$

$$5x^{-2} = 5 \times \frac{1}{x^2} = \frac{5}{\underline{\underline{x^2}}}$$

Example 1 – negative power

Rewrite $3x^{-4}$ and $5y^{-7}$ using positive powers

Solution

$$\frac{3}{\underline{\underline{x^4}}} \text{ and } \frac{5}{\underline{\underline{y^7}}}$$

A fraction as a power means a root. In general, $a^{\frac{m}{n}} = \sqrt[n]{a^m}$

$$\text{e.g. } 15^{\frac{2}{3}} = \sqrt[3]{15^2}, \quad a^{\frac{4}{3}} = \sqrt[3]{a^4}, \quad x^{\frac{1}{3}} = \sqrt[3]{x}$$

Example 2 – fraction power

Evaluate $9^{\frac{3}{2}}$ and $125^{\frac{4}{3}}$

Solution

$$9^{\frac{3}{2}} = \sqrt[2]{9^3}$$

$$= 3^3$$

$$= \underline{27}$$

$$125^{\frac{4}{3}} = \sqrt[3]{125^4}$$

$$= 5^4$$

$$= \underline{625}$$

Hint: calculate the root first and the power second, or the sum may prove too hard for you

Example 3 – negative and fractional powers

Simplify $25^{-\frac{1}{2}}$

Solution

$$25^{-\frac{1}{2}} = \frac{1}{25^{\frac{1}{2}}} \quad (\text{moving negative power to the bottom})$$

$$= \frac{1}{\sqrt{25}} \quad (\text{changing fractional power into surd})$$

$$= \frac{1}{\underline{\underline{5}}} \quad (\text{simplifying the surd})$$

Exercise 2

1. Rewrite the following with positive indices.

- | | | | | | | | | | | | |
|-----------|--------------------|------------|--------------------|------------|--------------------|------------|---------------------|------------|---------------------|------------|---------------------|
| a) | 3^{-2} | (b) | 5^{-4} | (c) | 2^{-6} | (d) | 10^{-3} | (e) | 4^{-5} | (f) | 200^{-7} |
| g) | a^{-5} | (h) | x^{-2} | (i) | p^{-7} | (j) | y^{-10} | (k) | $2b^{-3}$ | (l) | $10 q^{-x}$ |
| m) | $\frac{1}{x^{-3}}$ | (n) | $\frac{1}{w^{-5}}$ | (o) | $\frac{3}{a^{-2}}$ | (p) | $\frac{10}{c^{-8}}$ | (q) | $\frac{2}{3t^{-1}}$ | (r) | $\frac{5}{4y^{-3}}$ |

2. Rewrite the following with negative indices.

- | | | | | | | | | | | | |
|-----------|-----------------|------------|-----------------|------------|-----------------|------------|--------------------|------------|------------------|------------|-----------------|
| a) | $\frac{1}{3^2}$ | (b) | $\frac{1}{6^9}$ | (c) | $\frac{1}{5^4}$ | (d) | $\frac{1}{2^7}$ | (e) | $\frac{1}{10^3}$ | (f) | $\frac{1}{4^4}$ |
| g) | $\frac{1}{x^3}$ | (h) | $\frac{1}{a^5}$ | (i) | $\frac{1}{p^4}$ | (j) | $\frac{1}{y^{10}}$ | (k) | $\frac{1}{q^6}$ | (l) | $\frac{1}{c^8}$ |

3. Simplify the following expressions.

- | | | | | | | | | | |
|-----------|------------------------------------|------------|---------------------------------------|------------|---------------------------------------|------------|------------------------|------------|-----------------------|
| a) | $m^3 \times m^{-5}$ | (b) | $x^7 \times x^{-2}$ | (c) | $p^{-8} \times p^5$ | (d) | $a^{-3} \times a^{-5}$ | (e) | $(y^3)^{-4}$ |
| f) | $(c^{-5})^3$ | (g) | $(q^3)^{-5}$ | (h) | $(w^{-2})^{-4}$ | (i) | $4b^{-4} \times 5b^5$ | (j) | $3x^6 \times 9x^{-6}$ |
| k) | $4k^3 \div 2k^{-2}$ | (l) | $18d \div 12d^4$ | (m) | $x^2(x^3 + x^{-1})$ | (n) | $p^{-3}(p^4 - p^{-8})$ | | |
| o) | $3a^5(2a + 3a^{-2})$ | (p) | $\frac{1}{2} m^{-2}(4m^{-3} - 10m^6)$ | (q) | $\frac{v^3 \times v^5}{v^{-2}}$ | | | | |
| r) | $\frac{4h^7 \times 3h^{-4}}{2h^4}$ | (s) | $\frac{4c^{-5} \times 9c^6}{6c^{-4}}$ | (t) | $\frac{5x^4 \times 6x^{-8}}{3x^{-4}}$ | | | | |

4. Find the value of

- | | | | | | | | | | | | |
|-----------|----------------------|------------|-------------------------------|------------|---------------------|------------|----------------------|------------|----------------------|------------|-----------------------|
| a) | $16^{\frac{1}{4}}$ | (b) | $8^{\frac{1}{3}}$ | (c) | $36^{\frac{1}{2}}$ | (d) | $27^{\frac{2}{3}}$ | (e) | $64^{\frac{1}{3}}$ | (f) | $1000^{\frac{1}{3}}$ |
| g) | $25^{\frac{1}{2}}$ | (h) | $81^{\frac{3}{4}}$ | (i) | $125^{\frac{2}{3}}$ | (j) | $64^{\frac{1}{2}}$ | (k) | $216^{\frac{1}{3}}$ | (l) | $16^{-\frac{1}{4}}$ |
| m) | $4^{-\frac{1}{2}}$ | (n) | $16^{-\frac{1}{2}}$ | (o) | $9^{-\frac{1}{2}}$ | (p) | $27^{-\frac{2}{3}}$ | (q) | $256^{-\frac{3}{4}}$ | (r) | $1000^{-\frac{2}{3}}$ |
| s) | $16^{-\frac{3}{2}}$ | (t) | $8^{-\frac{4}{3}}$ | (u) | $8^{\frac{4}{3}}$ | (v) | $(-8)^{\frac{1}{3}}$ | (w) | $64^{\frac{2}{3}}$ | (x) | $100^{-\frac{3}{2}}$ |
| y) | $(\frac{1}{2})^{-1}$ | (z) | $(\frac{1}{8})^{\frac{4}{3}}$ | | | | | | | | |

5. Simplify the following expressions, giving your answers with positive indices.

- a)** $(x^{\frac{1}{2}})^6$ **(b)** $(p^{\frac{1}{3}})^6$ **(c)** $(a^{\frac{3}{4}})^8$ **(d)** $(y^{-\frac{2}{3}})^9$ **(e)** $(q^{-\frac{1}{5}})^{10}$ **(f)** $(k^{-\frac{2}{5}})^1$
- g)** $(g^4)^{\frac{1}{2}}$ **(h)** $(m^{12})^{-\frac{2}{3}}$ **i)** $(c^9)^{\frac{2}{3}}$ **(j)** $(h^5)^{-\frac{1}{2}}$ **(k)** $(z^4)^{-\frac{3}{4}}$ **(l)** $(b^{16})^{-\frac{3}{4}}$
- m)** $x^{\frac{1}{2}} \times x^{-\frac{1}{2}}$ **(n)** $y^{\frac{1}{3}} \times y^{\frac{2}{3}}$ **(o)** $d^{-\frac{1}{4}} \times d^{\frac{9}{4}}$ **(p)** $s^{\frac{7}{2}} \times s^{-\frac{1}{2}}$
- q)** $3x^{\frac{1}{2}} \times 4x^{\frac{1}{2}}$ **(r)** $6x^{\frac{1}{2}} \times 2x^{-\frac{1}{2}}$ **(s)** $2x^{\frac{1}{2}} \times 5x^{\frac{1}{2}}$ **(t)** $3x^{\frac{2}{3}} \times 2x^{-\frac{1}{3}}$
- u)** $x^{\frac{1}{2}} \div x^{\frac{1}{2}}$ **(v)** $2x^{\frac{1}{2}} \div x^{-\frac{1}{2}}$ **w)** $8x^{\frac{2}{3}} \div 2x^{\frac{1}{3}}$ **(x)** $6x^{\frac{1}{3}} \div 4x^{\frac{2}{3}}$

6. Write the following in surd form.

- a)** $x^{\frac{1}{2}}$ **(b)** $y^{\frac{1}{3}}$ **(c)** $a^{\frac{1}{4}}$ **(d)** $y^{\frac{2}{3}}$ **(e)** $b^{\frac{3}{4}}$ **(f)** $x^{\frac{5}{3}}$
- g)** $c^{\frac{3}{5}}$ **(h)** $a^{\frac{4}{5}}$ **(i)** $c^{-\frac{1}{3}}$ **(j)** $z^{-\frac{1}{2}}$ **(k)** $m^{-\frac{2}{3}}$ **(l)** $k^{-\frac{3}{5}}$
- m)** $p^{-\frac{4}{3}}$ **(n)** $x^{-\frac{5}{3}}$ **(o)** $w^{-\frac{4}{5}}$ **(p)** $d^{-\frac{2}{7}}$

7. Write the following in index form.

- a)** \sqrt{x} **(b)** $\sqrt[3]{a}$ **(c)** $\sqrt{y^3}$ **(d)** $\sqrt[3]{z^2}$ **(e)** $\sqrt[3]{c^2}$ **(f)** $\sqrt[4]{x^3}$
- g)** $\sqrt[3]{p^5}$ **(h)** $\sqrt[5]{m^2}$ **(i)** $\frac{1}{\sqrt{a}}$ **(j)** $\frac{1}{\sqrt[3]{z}}$ **(k)** $\frac{1}{\sqrt[3]{x^4}}$ **(l)** $\frac{1}{\sqrt[3]{a^5}}$
- m)** $\frac{1}{\sqrt[3]{b^2}}$ **(n)** $\frac{1}{\sqrt[5]{m^3}}$ **(o)** $\frac{1}{\sqrt[4]{y}}$ **(p)** $\frac{1}{\sqrt[3]{c^5}}$

8. Simplify each of the following by:

- (i) changing root signs to fractional powers;
- (ii) moving x 's onto the numerators;
- (iii) expanding brackets where necessary.

- a)** $x^{\frac{1}{2}}(x^4 + 1)$ **(b)** $x^{-\frac{1}{2}}(x^{\frac{3}{2}} - x^2)$ **(c)** $\frac{1}{x^2}(x^{\frac{1}{2}} + x)$ **(d)** $\frac{2}{x^{-3}}(x^2 + \frac{1}{x})$
- e)** $\frac{1}{\sqrt{x}}(x^2 - \sqrt{x})$ **(f)** $\left(x^2 + \frac{1}{x}\right)^2$ **(g)** $\frac{1}{x}(\sqrt{x} + x)$ **(h)** $\left(x + \frac{1}{\sqrt{x}}\right)^2$
- i)** $x^{-2}\left(\frac{1}{x} - \sqrt[3]{x}\right)$ **(j)** $\frac{x^2 + 3}{x}$ **(k)** $\frac{\sqrt{x} - x}{x^2}$ **(l)** $\frac{(2x+1)^2}{x^{\frac{3}{2}}}$

Mixed Exercise

1. a) Simplify $\frac{7a^3b^2}{a\sqrt{b}}$

b) If $a = -1$ and $b = 4$, find the value of the expression in part (a).

2. Given that $y = 2x^{-\frac{2}{3}}$, find y when $x = 8$.

3. Simplify $x^{\frac{2}{3}}(x^{\frac{2}{3}} + x^{-\frac{2}{3}})$

4. a) Simplify $\frac{m^5}{m^{-3}}$

b) Evaluate $125^{-\frac{2}{3}}$

5. Express $\frac{p^5 \times 8p}{2p^{-3}}$ in its simplest form.

6. Simplify, writing your answer with a positive index: $3a^4 \times a^{-6}$

7. Simplify the fraction, giving your answer in positive index form: $\frac{x^3 \times x^4}{x^9}$

8. Simplify $\frac{a^2 \times a^5}{a^{-3}}$.

9. a) Remove the brackets and simplify: $p^{\frac{1}{2}}(p^{\frac{5}{2}} - 2)$.

b) Hence, or otherwise, find the value of $p^{\frac{1}{2}}(p^{\frac{5}{2}} - 2)$ when $p = 4$.

Answers

Exercise 1

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|----|-------------|---------------|--------------|--------------|--------------|--------------|
| 1. | a) 3^6 | (b) 2^4 | (c) 10^7 | (d) 8^8 | (e) 7^7 | (f) 5^8 |
| | g) 9^8 | (h) 6^{13} | (i) x^8 | (j) c^{11} | (k) a^{14} | (l) y^{10} |
| | m) b^{40} | (n) p^{10} | (o) d^6 | (p) q^{20} | (q) t^{10} | (r) f^7 |
| | s) k^{13} | (t) z^{100} | (u) x^{80} | (v) y^{20} | (w) a^{90} | (x) b^1 |

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|----|-------------|-----------|------------|--------------|--------------|--------------|
| 2. | a) 2^5 | (b) 5^2 | (c) 12^3 | (d) 7^7 | (e) 20^4 | (f) 8^4 |
| | g) 3^{15} | (h) 4^2 | (i) x^5 | (j) a^4 | (k) y^{10} | (l) b^3 |
| | m) p | (n) 1 | (o) q^6 | (p) d^3 | (q) x^6 | (r) a^6 |
| | s) m^{13} | (t) 1 | (u) d^8 | (v) y^{90} | (w) t^{99} | (x) w^{10} |

- | | | | | | | |
|----|-------------|--------------|---------------|--------------|--------------|--------------|
| 3. | a) 3^8 | (b) 8^4 | (c) 10^6 | (d) 2^{10} | (e) 4^{15} | (f) 1 |
| | g) 12^9 | (h) 5^{25} | (i) x^8 | (j) y^{40} | (k) a^{21} | (l) m^{16} |
| | m) b^{18} | (n) p^{15} | (o) k^{100} | (p) 1 | | |

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|----|--------------|----------------|----------------|----------------|--------------------|----------------|
| 4. | a) $4b^2$ | (b) $343a^3$ | (c) $81x^4$ | (d) $32y^5$ | (e) a^4b^4 | (f) x^7y^7 |
| | g) w^5z^5 | (h) s^3t^3 | (i) p^3q^6 | (j) x^8y^2 | (k) $a^{10}b^{15}$ | (l) $36a^{10}$ |
| | m) $1000x^6$ | (n) $32c^{20}$ | (o) $27a^3b^6$ | (p) $16m^4k^2$ | | |

- | | | | | | |
|----|------------------|---------------------|---------------------|-----------------|----------------------------|
| 5. | a) $10a^8$ | (b) $63x^9$ | (c) $3p^3$ | (d) $5b^6$ | (e) $24y^7$ |
| | f) $80q^{10}$ | (g) $8c^7$ | (h) $8z^4$ | (i) $k^5 + k^7$ | (j) $m^7 - m^8$ |
| | k) $2x^7 + 6x^6$ | (l) $10a^7 - 15a^8$ | (m) x^3 | (n) m^{14} | (o) $10c^4$ |
| | p) $6q^3$ | (q) $3xy^{14}$ | (r) $4a^{10}b^{28}$ | (s) $4p^3$ | (t) $\frac{8}{3}a^2b^{12}$ |

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|----|--------|---------|---------|---------|---------|---------|
| 6. | a) 1 | (b) 1 | (c) 1 | (d) 1 | (e) 1 | (f) 1 |
| | g) 1 | (h) 1 | (i) 1 | (j) 1 | (k) 1 | (l) 1 |

Exercise 2

1. (a) $\frac{1}{3^2}$ (b) $\frac{1}{5^4}$ (c) $\frac{1}{2^6}$ (d) $\frac{1}{10^3}$ (e) $\frac{1}{4^5}$ (f) $\frac{1}{200^7}$

(g) $\frac{1}{a^5}$ (h) $\frac{1}{x^2}$ (i) $\frac{1}{p^7}$ (j) $\frac{1}{y^{10}}$ (k) $\frac{2}{b^3}$ (l) $\frac{10}{q^x}$

(m) x^3 (n) w^5 (o) $3a^2$ (p) $10c^8$ (q) $\frac{2}{3}t$ (r) $\frac{5}{4}y^3$

2. (a) 3^{-2} (b) 6^{-9} (c) 5^{-4} (d) 2^{-7} (e) 10^{-3} (f) 4^{-4}

(g) x^{-3} (h) a^{-5} (i) p^{-4} (j) y^{-10} (k) q^{-6} (l) c^{-8}

3. (a) m^{-2} (b) x^5 (c) p^{-3} (d) a^{-8} (e) y^{-12}

(f) c^{-15} (g) q^{-15} (h) w^8 (i) $20b$ (j) 27

(k) $2k^5$ (l) $1.5d^{-3}$ (m) $x^5 + x$ (n) $p - p^{-11}$ (o) $6a^6 + 9a^3$

(p) $2m^{-5} - 5m^4$ (q) v^{10} (r) $6h^{-1}$ (s) $6c^5$ (t) 10

4. (a) 2 (b) 2 (c) 6 (d) 9 (e) 4 (f) 10

(g) 5 (h) 27 (i) 25 (j) 8 (k) 6 (l) $\frac{1}{2}$

(m) $\frac{1}{2}$ (n) $\frac{1}{4}$ (o) $\frac{1}{3}$ (p) $\frac{1}{9}$ (q) $\frac{1}{64}$ (r) $\frac{1}{100}$

(s) $\frac{1}{64}$ (t) $\frac{1}{16}$ (u) 16 (v) -2 (w) 16 (x) $\frac{1}{1000}$

(y) 2 (z) $\frac{1}{16}$

5. a) x^3 (b) p^2 (c) a^6 (d) $\frac{1}{y^6}$ (e) $\frac{1}{q^2}$ (f) $\frac{1}{k^{\frac{2}{5}}}$

g) g^2 (h) $\frac{1}{m^8}$ (i) c^6 (j) $\frac{1}{h^{\frac{5}{2}}}$ (k) $\frac{1}{z^3}$ (l) $\frac{1}{b^{12}}$

m) 1 (n) y (o) d^2 (p) s^3 (q) $12x$ (r) 12

s) $10x$ (t) $6x^{\frac{1}{3}}$ (u) 1 (v) $2x$ (w) $4x^{\frac{1}{3}}$ (x) $\frac{3}{2x^{\frac{1}{3}}}$

6. a) \sqrt{x} (b) $\sqrt[3]{x}$ (c) $\sqrt[4]{a}$ (d) $\sqrt[3]{y^2}$ (e) $\sqrt[4]{b^3}$ (f) $\sqrt[3]{x^5}$

g) $\sqrt[5]{c^3}$ (h) $\sqrt[5]{a^4}$ (i) $\frac{1}{\sqrt[3]{c}}$ (j) $\frac{1}{\sqrt{z}}$ (k) $\frac{1}{\sqrt[3]{m^2}}$ (l) $\frac{1}{\sqrt[5]{k^3}}$

m) $\frac{1}{\sqrt[3]{p^4}}$ (n) $\frac{1}{\sqrt[3]{x^5}}$ (o) $\frac{1}{\sqrt[5]{w^4}}$ (p) $\frac{1}{\sqrt[7]{d^2}}$

7. a) $x^{\frac{1}{2}}$ (b) $a^{\frac{1}{3}}$ (c) $y^{\frac{3}{2}}$ (d) $z^{\frac{2}{3}}$ (e) $c^{\frac{2}{3}}$ (f) $x^{\frac{3}{4}}$

g) $p^{\frac{5}{3}}$ (h) $m^{\frac{2}{5}}$ (i) $a^{-\frac{1}{2}}$ (j) $z^{-\frac{1}{3}}$ (k) $x^{-\frac{4}{3}}$ (l) $a^{-\frac{1}{5}}$

m) $b^{-\frac{2}{3}}$ (n) $m^{-\frac{3}{5}}$ (o) $y^{-\frac{1}{4}}$ (p) $c^{-\frac{5}{3}}$

8. a) $x^{\frac{9}{2}} + x^{\frac{1}{2}}$ (b) $x - x^{\frac{3}{2}}$ (c) $x^{-\frac{3}{2}} + x^{-1}$ (d) $2x^5 + 2x^2$

e) $x^{\frac{3}{2}} - 1$ (f) $x^4 + 2x + \frac{1}{x^2}$ (g) $x^{-\frac{1}{2}} + 1$ (h) $x^2 + 2x^{\frac{1}{2}} + x^{-1}$

(i) $x^{-3} - x^{-\frac{5}{3}}$ (j) $x + 3x^{-1}$ (k) $x^{-\frac{3}{2}} - x^{-1}$ (l) $4x^{\frac{1}{2}} + 4x^{-\frac{1}{2}} + x^{-\frac{3}{2}}$

Mixed Exercise

1. a) $7a^2b^{\frac{3}{2}}$ (b) 56 2. $\frac{1}{2}$ 3. $x^{\frac{4}{3}} + 1$

4. a) m^8 (b) $\frac{1}{25}$ 5. $4p^9$ 6. $\frac{3}{a^2}$

7. $\frac{1}{x^2}$ 8. a^{10} 9. a) $p^3 - 2p^{\frac{1}{2}}$ (b) 60