

Higher Grade Unit Tests

Marking Scheme - UNIT 1

	Give 1 mark for each •	Illustration(s) for awarding each mark
1	D	
2	B	
3	C	Award 2 marks for each correct answer
4	B	10 marks
5	A	
6(a)	ans: $y + 2x = 7$ (3 marks)	<p>—¹ knows to find gradient of AB</p> <p>—² finds gradient</p> <p>—³ substitutes values in equation</p> <p>—¹ $m_{AB} = \frac{y_2 - y_1}{x_2 - x_1}$</p> <p>—² $m_{AB} = \frac{-2 - 2}{-3 + 5} = -2$</p> <p>—³ $y + 1 = -2(x - 4)$</p>
(b)	ans: $y + 7x = -33$ (3 marks)	<p>—¹ finds gradient of BC</p> <p>—² takes perpendicular gradient</p> <p>—³ substitutes values in equation</p> <p>—¹ $m_{BC} = \frac{-1 + 2}{4 + 3} = \frac{1}{7}$</p> <p>—² $m_{PERP} = -7$</p> <p>—³ $y - 2 = -7(x + 5)$</p>
(c)	ans: (-8, 23) (4 marks)	<p>—¹ knows to use simultaneous equations</p> <p>—² finds value for x</p> <p>—³ finds value for y</p> <p>—⁴ states coordinates</p> <p>—¹ evidence</p> <p>—² $x = -8$</p> <p>—³ $y = 23$</p> <p>—⁴ (-8, 23)</p>
7(a)	ans: $-x$ (2 marks)	<p>—¹ substitutes</p> <p>—² simplifies</p> <p>—¹ $g(3 - x)$</p> <p>—² $3 - x - 3 = -x$</p>
(b)	ans: proof (2 marks)	<p>—¹ finds expression for $f(g(x))$</p> <p>—² simplifies to answer</p> <p>—¹ $3 - (x - 3) = 3 - x - 3 = 6 - x$</p> <p>—² $-x - (6 - x) = -6$</p>

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8(a)	ans: $a = 0.8$; $b = -2$ (3marks)	$\begin{array}{l} \text{---}^1 \text{ forms a system of equations} \\ \text{---}^2 \text{ finds value for } a \\ \text{---}^3 \text{ finds value for } b \end{array}$ $\begin{array}{l} \text{---}^1 9 \cdot 2 = 14a + b; 5 \cdot 36 = 9 \cdot 2a + b \\ \text{---}^2 a = 0.8 \\ \text{---}^3 b = -2 \end{array}$
(b)	ans: $-1 < 0.8 < 1$ (1 mark)	$\begin{array}{l} \text{---}^1 \text{ states condition for limit} \end{array}$ $\begin{array}{l} \text{---}^1 -1 < 0.8 < 1 \end{array}$
(c)	ans: 20 (2 marks)	$\begin{array}{l} \text{---}^1 \text{ substitutes for } U_2 \\ \text{---}^2 \text{ solves for } U_1 \end{array}$ $\begin{array}{l} \text{---}^1 U_2 = 0.8 U_1 - 2; 14 = 0.8 U_1 - 2 \\ \text{---}^2 0.8 U_1 = 16; U_1 = 20 \end{array}$
9	ans: $y = 9x - 16$ (5 marks)	$\begin{array}{l} \text{---}^1 \text{ knows to differentiate} \\ \text{---}^2 \text{ finds derivative} \\ \text{---}^3 \text{ substitutes } x = 2 \text{ in derivative} \\ \text{---}^4 \text{ finds point on the line} \\ \text{---}^5 \text{ substitutes in equation} \end{array}$ $\begin{array}{l} \text{---}^1 \frac{dy}{dx} = \\ \text{---}^2 3x^2 - 3 \\ \text{---}^3 3(2)^2 - 3 = 9 \\ \text{---}^4 y = (2)^3 - 3(2) = 8 - 6 = 2; (2, 2) \\ \text{---}^5 y - 2 = 9(x - 2) \end{array}$
10	ans: $3(x - 1)^2 + 8$ (3marks)	$\begin{array}{l} \text{---}^1 \text{ takes common factor} \\ \text{---}^2 \text{ completes square in bracket} \\ \text{---}^3 \text{ simplifies} \end{array}$ $\begin{array}{l} \text{---}^1 3(x^2 - 2x) + 11 \\ \text{---}^2 3[(x - 1)^2 - 1] + 11 \\ \text{---}^3 3(x - 1)^2 - 3 + 11 = 3(x - 1)^2 + 8 \end{array}$
11(a)	ans: $k = 3$ (1 mark)	$\begin{array}{l} \text{---}^1 \text{ substitutes and solves for } k \end{array}$ $\begin{array}{l} \text{---}^1 k = \log_5 125; k = 3 \end{array}$
(b)	ans: $a = 3$ (1 mark)	$\begin{array}{l} \text{---}^1 \text{ substitutes and solves for } a \end{array}$ $\begin{array}{l} \text{---}^1 9 = a^2; a = 3 \end{array}$

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(a)	ans: proof (2 marks) <ul style="list-style-type: none"> –¹ finds expression for S.A. –² rearranges to answer 	$\begin{aligned} & -^1 \quad x^2 + 4xh = 1350 \\ & -^2 \quad 4xh = 1350 - x^2 ; h = \frac{1350 - x^2}{4x} \end{aligned}$
(b)	ans: proof (3 marks) <ul style="list-style-type: none"> –¹ finds expression for volume –² cancels –³ completes rearranging 	$\begin{aligned} & -^1 \quad V = x \times x \times \left(\frac{1350 - x^2}{4x} \right) \\ & -^2 \quad V = x \times \left(\frac{1350 - x^2}{4} \right) \\ & -^3 \quad V = \frac{1}{4}x(1350 - x^2) \end{aligned}$
(c)	ans: $15\sqrt{2}$ (5 marks) <ul style="list-style-type: none"> –¹ knows to differentiate and equal 0 –² differentiates –³ solves for x –⁴ expresses as a surd –⁵ justifies answer 	$\begin{aligned} & -^1 \quad \frac{dV}{dx} = 0 \\ & -^2 \quad \frac{1350}{4} - \frac{3}{4}x^2 \\ & -^3 \quad x = \sqrt{450} \\ & -^4 \quad 15\sqrt{2} \\ & -^5 \quad \text{or other acceptable method} \end{aligned}$ <p style="text-align: right;">↗ → ↘</p>