St Peter the Apostle High

Mathematics Dept.

Higher Prelim Revision 5

Paper I - Non~calculator

Time allowed - 1 hour 30 minutes

Section A - Questions 1 - 20 (40 marks)

Instructions for the completion of **Section A** are given on the next page. For this section of the examination you should use an **HB pencil**.

Section B (30 marks)

- 1. Full credit will be given only where the solution contains appropriate working.
- 2. Answers obtained by readings from scale drawings will not receive any credit.

FORMULAE LIST

Circle:

The equation $x^2 + y^2 + 2gx + 2fy + c = 0$ represents a circle centre (-g, -f) and radius $\sqrt{g^2 + f^2 - c}$.

The equation $(x-a)^2 + (y-b)^2 = r^2$ represents a circle centre (a, b) and radius r.

Trigonometric formulae: $sin(A \pm B) = sin A cos B \pm cos A sin B$ $cos(A \pm B) = cos A cos B \mp sin A sin B$ sin2A = 2sin A cos A $cos2A = cos^{2} A - sin^{2} A$ $= 2 cos^{2} A - 1$ $= 1 - 2 sin^{2} A$

Read carefully

- 1 Check that the answer sheet provided is for Mathematics Higher Prelim 2007/2008 (Section A).
- 2 For this section of the examination you must use an **HB pencil** and, where necessary, an eraser.
- 3 Make sure you write your **name**, **class** and **teacher** on the answer sheet provided.
- 4 The answer to each question is **either** A, B, C or D. Decide what your answer is, then, using your pencil, put a horizontal line in the space below your chosen letter (see the sample question below).
- 5 There is **only one correct** answer to each question.
- 6 Rough working should **not** be done on your answer sheet.
- 7 Make sure at the end of the exam that you hand in your answer sheet for Section A with the rest of your written answers.

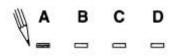
Sample Question

A line has equation y = 4x - 1.

If the point (k,7) lies on this line, the value of k is

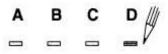
A	2
B	27
С	1.5
D	- 2

The correct answer is $\mathbf{A} \rightarrow 2$. The answer \mathbf{A} should then be clearly marked in pencil with a horizontal line (see below).



Changing an answer

If you decide to change an answer, carefully erase your first answer and using your pencil, fill in the answer you want. The answer below has been changed to D.



SECTION A ALL questions should be attempted

1.	If $f(x) = 2x^{\frac{3}{2}}$ then	f'(4) equals		
	A 16	B 4	C $25\frac{3}{5}$	D 6
2.	The gradient of the a	0	C $-\frac{3}{8}$	$\mathbf{D} = \frac{8}{3}$
3.	The remainder when A 52	$x^3 - 11x + 10$ is divided by B 16	y $(x+3)$ is C 4	D −24

5. A sequence is defined by the recurrence relation $U_{n+1} = aU_n - 5$ with $U_0 = 10$. An expression in terms of *a* for U_2 is

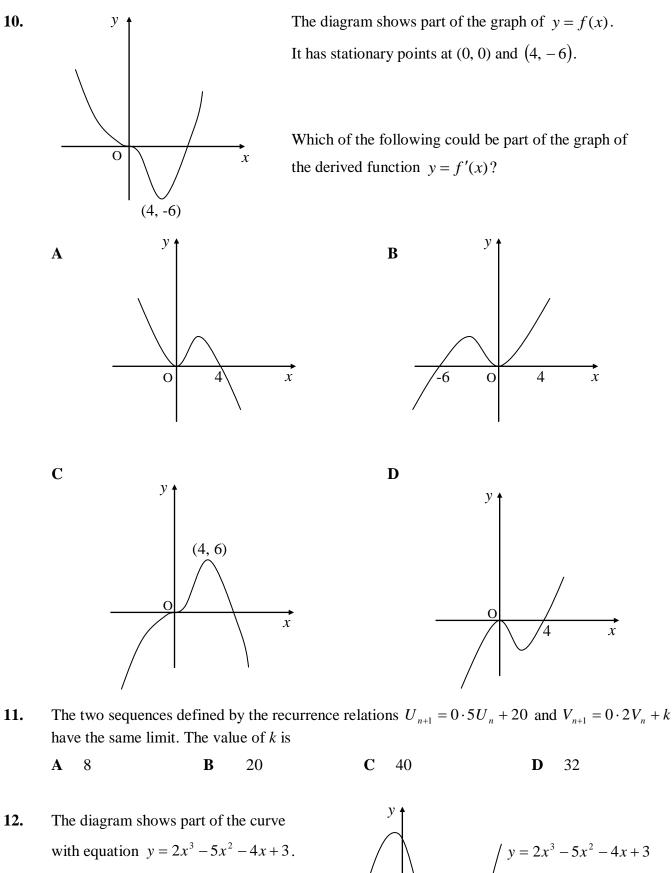
B

A 10a - 5

6. $\int_{0}^{1} 4x(x^2-2) dx$ is A -3 B -4 C 0 D 12

 $10a^2 - 5$ **C** $10a^2 - 5a - 5$ **D** $10a^2$

- 7. The equation $2x^2 + 8 = kx$ has no real roots. k must take the values A ± 8 B -8 < k < 8 C k < -8 or k > 8 D undefined
- 8. For which value(s) of x is the function $f(x) = \frac{3}{(x+3)(x-2)}$ undefined? A 3 B 3 and -2 C -3 and 2 D -6
- 9. The line ax-2y+5=0 is parallel to the line with equation 3x+y-4=0. The value of *a* is
 - **A** -3 **B** -6 **C** $\frac{2}{3}$ **D** $-\frac{3}{2}$



0

A

x

The *x*- coordinate of the point A is

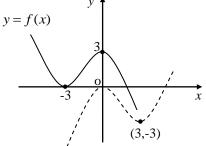
- $\mathbf{A} \quad \frac{1}{3} \qquad \qquad \mathbf{B} \quad 2$
- **C** 3 **D** -9

13. The function f is defined as $f(x) = \frac{x-6}{x}$, $x \neq 0$. The value of f(f(3)) equals A 7 B -7 C -5 D -1

14. The diagram shows the graph of y = f(x) as a full line and the graph of a related function as a broken line. The equation of the related function is $y \uparrow$

A
$$y = -f(x) - 3$$

B $y = f(x-6) - 3$
C $y = f(-x) - 3$
D $y = f'(x)$



 $\frac{\sqrt{3}}{4}$

17. The maximum value of $\frac{12}{x^2 - 4x + 10}$ is



18. A ball is thrown upwards reaching a height of 'h' metres after 't' seconds where $h(t) = 2 + 12t - 3t^2$. The time taken, in seconds, to reach its maximum height is **A** 2 **B** 3 **C** 4 **D** 5

19. The exact value of $\sin \frac{2\pi}{3} - \cos \frac{7\pi}{6}$ is

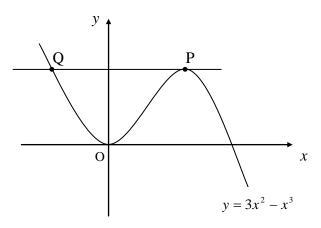
A 0 **B** 1 **C** $\sqrt{3}$ **D**

20.	(x, y) is a solution for the system of equations	$x^2 + 7y^2 = 16$	
		x-3y=0.	
	Possible values for $x + y$ are		
	(1) 0 (2) 4 (3) -4		
	A (1) only B (2) only	C (2) and (3) only	D (1), (2) and (3)

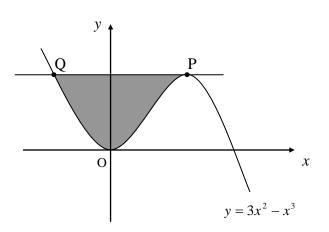
[END OF SECTION A]

SECTION B ALL questions should be attempted

21. Part of the graph of the curve with equation $y = 3x^2 - x^3$ is shown below. The diagram is not drawn to scale.



- (a) Establish the coordinates of the stationary point P.
- (b) The horizontal line through P meets the curve again at Q. Find the coordinates of Q.
- (c) Hence calculate the shaded area shown in the diagram below.

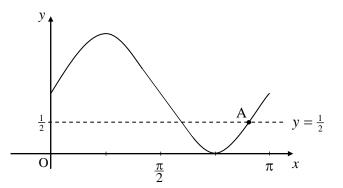


4

3

6

- 22. Two functions, defined on suitable domains, are given as $f(x) = x^2 1$ and g(x) = 2 x.
 - (a) Show that f(g(a)) can be expressed in the form $pa^2 + qa + r$ and write down the values of p, q and r.
 - (b) Hence find a if f(g(a)) = 8 and a > 0.
- 23. The diagram below shows part of the graph of $y = \sin 2x + 1$, for $0 \le x \le \pi$, and the line with equation $y = \frac{1}{2}$.



Find the coordinates of the point A.

24. A recurrence relation is defined by the formula $U_{n+1} = 0.6U_n + 24$.

(a)	Establish the limit of this sequence.	2
(b)	Given now that U_1 is exactly half of this limit, find U_0 , the initial value of the sequence.	2
(c)	A second recurrence relation in the form $U_{n+1} = aU_n + b$ has the same limit as the sequence above and is such that $b = 90a$.	

Find the values of a and b in this second sequence.

[END OF SECTION B]

[END OF QUESTION PAPER]

4

3

4

2