Mathematics Practice Paper H Paper 1 Assessing Units 1, 2 & 3 NATIONAL QUALIFICATIONS

Time allowed - 1 hour 30 minutes

### **Read carefully**

Calculators may <u>NOT</u> be used in this paper.

Section A - Questions 1 - 20 (40 marks)

Instructions for the completion of Section A are given on the next page.

For this section of the examination you should use an HB pencil.

# Section B (30 marks)

- 1. Full credit will be given only where the solution contains appropriate working.
- 2. Answers obtained by readings from scale drawings will not receive any credit.

#### FORMULAE LIST

The equation  $x^2 + y^2 + 2gx + 2fy + c = 0$  represents a circle centre (-g, -f) and radius  $\sqrt{(g^2 + f^2 - c)}$ .

The equation  $(x-a)^2 + (y-b)^2 = r^2$  represents a circle centre (a, b) and radius r.

Scalar Product:  $a \cdot b = |a| |b| \cos\theta$ , where  $\theta$  is the angle between a and b.

or  

$$a \cdot b = a_1 b_1 + a_2 b_2 + a_3 b_3$$
 where  $a = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix}$  and  $b = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$ 

Trigonometric formulae:

$$\sin (A \pm B) = \sin A \cos B \pm \cos A \sin B$$
$$\cos (A \pm B) = \cos A \cos B \mp \sin A \sin B$$
$$\cos 2A = \cos^2 A - \sin^2 A$$
$$= 2\cos^2 A - 1$$
$$= 1 - 2\sin^2 A$$
$$\sin 2A = 2\sin A \cos A$$

Table of standard derivatives:

f(x)	f'(x)
sin <i>ax</i>	$a \cos ax$
$\cos ax$	$-a \sin ax$

Table of standard integrals:

$$f(x) \qquad \int f(x) \, dx$$

$$\sin ax \qquad -\frac{1}{a}\cos ax + C$$
$$\cos ax \qquad \frac{1}{a}\sin ax + C$$

#### All questions should be answered

## Section A

1. Triangle PQR has vertices P(4, 7), Q(-2, 3) and R(2, 9). PM is a median of this triangle. The coordinates of M are

A.	(3, 8)
B.	(0, 6)
C.	(1, 5)
D.	(2, 6)

2. The sequence defined by the recurrence relation  $U_{n+1} = aU_n + 6$  has limit 10. The value of *a* is

A.	$2 \cdot 5$
B.	0.6
C.	$0 \cdot 4$
D.	$-0\cdot 4$

3. A function f is defined as  $f(x) = 3 - \frac{6}{x}$ . The value of f(f(-2)) is A. 0 B. 2 C. 3 D. 6

4. A circle has equation  $x^2 + y^2 - 6x + 8y - 1 = 0$ . The centre of it is

A.(6, 8)B.(-3, 4)C.(3, -4)D.(-6, 8)

5. Which of the following is **NOT** a factor of the equation  $x^3 - 4x^2 + x + 6 = 0$ .

A. (x+1)B. (x-2)C. (x+3)D. (x-3) 6. The diagram shows part of the graphs of y = f(x) and y = g(x). The curves intersect at the point (2, -1) and the origin.



The area enclosed by the two curves is given by

A. 
$$\int_{0}^{2} (g(x) - f(x)) dx$$
  
B.  $\int_{0}^{2} (g(x) + f(x)) dx$   
C.  $\int_{0}^{2} (g(x) \times f(x)) dx$   
D.  $\int_{0}^{2} (f(x) - g(x)) dx$ 

7. The exact value of 
$$\sin(\frac{11\pi}{6})$$
 equals  
A.  $\frac{1}{2}$   
B.  $-\frac{1}{2}$   
C.  $\frac{\sqrt{3}}{2}$   
D.  $-\frac{\sqrt{3}}{2}$ 

8. A sequence is defined by  $U_{n+1} = 1 \cdot 5U_n - 2$  with  $U_0 = 12$ . The value of  $U_3$  is

A.	69
B.	38
C.	31
D.	22

9. The point (81, k) lies on the graph  $y = \log_3 x$ . The value of k is

**A.**  $\frac{1}{4}$  **B.**  $3^{81}$  **C.** 27 **D.** 4

10. The exact value of  $2\sin 75^{\circ}\cos 75^{\circ}$  is

**A.** 
$$-\frac{1}{2}$$
  
**B.**  $\frac{1}{2}$   
**C.**  $\frac{\sqrt{3}}{2}$   
**D.**  $-\frac{\sqrt{3}}{2}$ 

11. The integral of  $\sqrt{(1+4x)} dx$  is

A. 
$$\frac{2}{3}(1+4x)^{\frac{3}{2}} + C$$
  
B.  $\frac{2}{(1+x)^{\frac{1}{2}}} + C$   
C.  $\frac{1}{6}(1+4x)^{\frac{3}{2}} + C$   
D.  $\frac{1}{2}(1+4x)^{\frac{3}{2}} + C$ 

12. The magnitude of vector  $\boldsymbol{g}$ , where  $\boldsymbol{g} = 7\boldsymbol{i} + 3\sqrt{5}\boldsymbol{j} - 5\sqrt{2}\boldsymbol{k}$ , is

**A.** 12 **B.**  $5\sqrt{3}$  **C.** 2 **D.**  $\sqrt{2}$ 

- 13. The derivative of  $(4-x)^4$  with respect to x is
  - A.  $-\frac{1}{5}(4-x)^5$ B.  $-4(4-x)^3$ C.  $-3(4-x)^3$ D.  $4(4-x)^3$
- 14. Given that (x+3) is a factor of  $x^3 5ax 3$ , the value of *a* is

А.	$\frac{2}{5}$
B.	$\frac{1}{2}$
C.	2
D.	$-\frac{2}{5}$

15. A parabola has equation  $y = x^2 - 10x + 16$ . The coordinates and nature of its turning point are

- A. (-5, -9) and maximum
  B. (-5, -9) and minimum
  C. (5, -9) and maximum
  D. (5, -9) and minimum
- 16. The curve with equation  $y = 2x^3 5x^2 4x + 3$  has 2 turning points one of which is minimum. The *x* - coordinate of this minimum turning point is

**A.** 
$$-\frac{1}{3}$$
  
**B.** 2  
**C.** -2  
**D**  $\frac{1}{3}$ 

17. The maximum value of  $\frac{1}{x^2 + 6x - 3}$  is

**A.** 
$$-\frac{1}{3}$$
  
**B.** 12  
**C.**  $\frac{1}{12}$   
**D.**  $-\frac{1}{12}$ 

18.  $\int 2\sin(3x+1) dx$  equals

A.  $\frac{2}{3}\cos(3x+1) + C$ B.  $6\cos(3x+1) + C$ C.  $-\frac{2}{3}\cos(3x+1) + C$ D.  $2\cos(3x+1) + C$ 

**19.** P is the point (-4, -1, -2) and R is the point (5, 8, 7). The point T divides PR in the ratio 5 : 4. The coordinates of T are

А.	(1, 7, 5)
B.	(1, 4, 3)
C.	(1, 1, 1)
D.	(-1, -4, -3)

20. When  $3\sin x + \cos x$  is expressed in the form  $k\cos(x-a)$ , the value of k and the range of values for a are

A. 
$$k = 2$$
 and  $\frac{\pi}{2} \le a \le \pi$   
B.  $k = \sqrt{10}$  and  $\frac{\pi}{2} \le a \le \pi$   
C.  $k = 2$  and  $0 \le a \le \frac{\pi}{2}$   
D.  $k = \sqrt{10}$  and  $0 \le a \le \frac{\pi}{2}$ 

# Section **B**

- 21. Part of the line with equation x + 3y = 9 is *Y* shown in the diagram. B lies on this line x + 3y = 9and has coordinates (3, 2). B(3, 2) 0 Given that the line AB is perpendicular (a) x to the line x + 3y = 9, find the equation of the line AB. 3 Hence write down the coordinates of A. (b) 1 Calculate the area of the shaded triangle. (c) 4
- What can you say about p if the equation, in x,  $\frac{x}{p} + \frac{9}{px} = 1$  has **no real** roots? 22. 6
- With reference to an origin O, the coordinates of A and B are (1,2,3) and 23. (4,1,5) respectively.
  - Prove that triangle OAB is isosceles. (a)
  - (b) Calculate the size of angle AOB.
- The diagram below shows two congruent circles which touch at a single point T. 24. The circle, centre A, has as its equation  $x^2 + y^2 - 6x - 18y + 45 = 0$ . The line with equation 2y = x is the common tangent to the two circles through T.



- Show algebraically that T has coordinates (6,3). (a)
- Hence establish the the coordinates of B, the centre of the lower circle, and (b) find the equation of this circle.

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