	Question	Answor
	<u>Question</u> 1	<u>Answer</u> C
	2	В
	3	D
	4	Α
	5	С
	6	В
	7	С
	8	D
	9	В
	10	D
	11	C
	12	C
	13	В
	14	D
	15	Α
	16	В
	17	D
	18	C
	19	В
	20	Α
Summary	Α	3
	В	6
	C	6
	D	5

## Paper 1 - Section B

Question	Generic Scheme	Illustrative Scheme	Max Mark
21(a).			
• <sup>1</sup> know to use	x = 1	Method 1 • $^{1} 1^{3} - 6(1)^{2} + 9(1) - 4$	
• <sup>2</sup> interpret res	sult and state conclusion	• <sup>2</sup> = 0 : $(x-1)$ is a factor.	
		Method 2 • <sup>1</sup>	
		$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
		• <sup>2</sup> 1 $\begin{vmatrix} 1 & -6 & 9 & -4 \\ \hline 1 & -5 & 4 \\ \hline 1 & -5 & 4 & 0 \\ remainder = 0 : (x-1) is a factor.$	
		Method 3 $x^{2}$ • $1 x - 1 \overline{\smash{\big)} x^{3} - 6x^{2} + 9x + 4}$ $x^{3} - x^{2}$ • $2 = 0 \therefore (x - 1)$ is a factor.	
• <sup>3</sup> state quadra	itic factor	• $x^{2}-5x+4$ stated or implied by • $4$	
• <sup>4</sup> factorise co	npletely	• $(x-1)^2(x-4)$	4

## Notes:

- 1. Communication at  $\bullet^2$  must be consistent with working at that stage i.e. a candidate's working must arrive legitimately at 0 before  $\bullet^2$  is awarded.
- 2. Accept any of the following for  $\bullet^2$ :
  - f(1) = 0 so (x-1) is a factor '
    - 'since remainder is 0, it is a factor'
    - the 0 from the table linked to the word 'factor' by e.g. 'so', 'hence', ' $\therefore$ ', ' $\rightarrow$ ', ' $\Rightarrow$ '
- 3. Do not accept any of the following for  $\bullet^2$ :
  - double underlining the zero or boxing the zero without comment
  - 'x = 1 is a factor', '(x+1) is a factor', 'x = 1 is a root', '(x+1) is a root', "(x-1) is a root"
  - the word 'factor' **only**, with no link
- 4. At •<sup>4</sup> the expression may be written as (x-1)(x-1)(x-4) in any order.
- 5. An incorrect quadratic correctly factorised may gain  $\bullet^4$ .
- 6. Where the quadratic factor obtained is irreducible, candidates must clearly demonstrate that  $b^2 4ac < 0$  to gain  $\bullet^4$ .
- 7. = 0 must appear at  $\bullet^1$  or  $\bullet^2$  for  $\bullet^2$  to be awarded.
- 8. For candidates who do not arrive at 0 at the  $\bullet^2$  stage  $\bullet^2 \bullet^3 \bullet^4$  are not available.
- 9. Do not penalise candidates who attempt to solve a cubic equation. However, within this working there may be evidence of the correct factorisation of the cubic.
- 10. Evidence for  $\bullet^3 \& \bullet^4$  may appear in part (b).

Commonly Observed Responses:

Question	Generic Scheme	Illustrative Scheme	Max Mark
21(b)(i).			
● <sup>5</sup> know to	and differentiate	• $5 3x^2 - 12x + 11$	
• <sup>6</sup> find grad	diant	• 6 2	
		• 2	
• <sup>7</sup> state eq	uation of tangent	• <sup>7</sup> $y=2x+1$	3
Notes:			
diff 12. At r	s only available if an attempt has been erentiation. nark $\bullet^7$ accept $y-3=2(x-1)$ , $y-2x=$ ation.	-	ne
	Observed Responses:		
Candidate			
• <sup>5</sup> $\checkmark$ • <sup>6</sup> using $y = m$ x = 1 $y = 3\Rightarrow 3 = 2 \times 1 + 3\Rightarrow c = 1y = 2x + 1$	$ \begin{array}{l}     ax + c \\     m = 2 \\     + c \end{array} $		
21(b)(ii).		T	1
	equation in standard cubic form <i>x</i> coordinate of B and calculate <i>y</i>	• <sup>8</sup> $x^3 - 6x^2 + 11x - 3 = 2x + 1$ • <sup>9</sup> $x^3 - 6x^2 + 9x - 4 = 0$ • <sup>10</sup> (4,9)	3
Notes:			
14. Solu 15. Can una 16. For	s only available if ${}^{\circ}=0$ appears in at utions at ${}^{10}$ must be consistent with w didates who obtain three distinct factor vailable. ${}^{10}$ accept $x = 4, y = 9$ . not penalise the appearance of $(1,3)$ .	vorking at $\bullet^4$ and $\bullet^7$ .	ion.
	Observed Responses:		
commonty			

Question	Generic Scheme	Illustrative Scheme	Max Mark
22.			
• <sup>1</sup> arrange in	differentiable form	$\bullet^1 f(x) = 4x^{-2} + x$	
• <sup>2</sup> start diffe	rentiation	• $^{2}$ -8 $x^{-3}$ or 1	
• <sup>3</sup> complete	differentiation and set $f'(x) = 0$	• $^{3} -8x^{-3} + 1 = 0$	
• <sup>4</sup> evaluate <i>f</i>	at stationary point	$\bullet^4 x = 2, f(x) = 3$	
<ul> <li><sup>5</sup> consider e</li> </ul>	nd-points	• <sup>5</sup> $f(1) = 5$ , $f(4) = \frac{17}{4}$ (or $4 \cdot 25$ )	
• <sup>6</sup> state max	and min values	• <sup>6</sup> max 5, min 3	6
Notes:			
1. Candidates must attempt to differentiate a term with a -ve or fractional power by $\bullet^3$ for $\bullet^3$ to be awarded.			
2. $\bullet^3$ is not available for simply stating ' $f'(x) = 0$ '. A clear link between the candidates			
derivative and ' $f'(x) = 0$ 'is required.			

- 3. For candidates who integrate, but clearly believe they are finding the derivative  $\bullet^1 \bullet^4 \bullet^5 \bullet^6$  are available (see CORs K, L, and M). In other instances where candidates have integrated then only  $\bullet^1$  and  $\bullet^5$  are available. A numerical approach can only gain  $\bullet^5$ .
- 4.  $\bullet^5$  and  $\bullet^6$  are not available to candidates who consider stationary points only.
- 5. Treat maximum (1,5) and minimum (2,3) as bad form.
- 6. Vertical marking is **not** applicable to  $\bullet^5$  and  $\bullet^6$ .
- 7. The appearance of (2,3) following any 2nd derivative or nature table gains  $\bullet^4$ .
- 8. If at the  $\bullet^4$  stage a value of x is obtained outwith the given interval then  $\bullet^4$  is unavailable, but  $\bullet^6$  may still be gained (see CORs F and G).
- 9. Candidates who consider the end values but do not evaluate the stationary value cannot gain  $\bullet^6$ .

Commonly Observed Responses:			
Candidate A	Candidate B	Candidate C	Candidate D
$f(x) = 4x^{-2} + x$ $f'(x) = -8x^{-3} + 1 \stackrel{\bullet^1}{\bullet^2} \checkmark$ for stationary	$f(x) = 4x^{-2} + x  \bullet^1  \checkmark \\ \bullet^2  \land$	$f(x) = 4x^{-2} + x  \bullet^{1} \checkmark$ $f'(x) = -8x^{-3} + 1  \bullet^{2} \checkmark$	$f(x) = 4x^{-2} + x  \bullet^{1} \checkmark$ $-8x^{-3} + 1  \bullet^{2} \checkmark$ for stationary $\bullet^{3} \land$
for stationary $\begin{pmatrix} 2 \\ 0 \\ 0 \end{pmatrix}$		for stationary $\bullet^3 \land$	for stationary
	for stationary points $f'(x) = 0$ With po further	points $\frac{dy}{dx} = 0$	points $f'(x) = 0$
With no further working	With no further working	With no further working	With no further working

Candidate E	Candidate F	Candidate G
Solely a numerical attempt		
f(1) = 5, f(2) = 3,	$f(x) = 4x^{-2} + x$ f'(x) = 8x	$f(x) = 4x^{-2} + x$ f'(x) = -8x
$f(3) = \frac{31}{9}, f(4) = \frac{17}{4}$	$f'(x) = 1 = 0  \bullet^1 \checkmark$	f'(x) = -1 - 0 - 1
Award only • <sup>5</sup> ✓	$f(x) = \dots + 1 = 0$ $x = -\frac{1}{8}  f(-\frac{1}{8}) = 255 \frac{7}{8} \cdot \frac{3}{4} \cdot \frac{3}{4}$	$x = \frac{1}{8} f(\frac{1}{8}) = 256\frac{1}{8} = \frac{1}{8} \frac{1}{8}$
For any similar attempt which includes the	$f(1) = 5, f(4) = 4\frac{1}{4}$ • • • • • • • • • • • • • • • • • • •	_ <sup>0</sup> ✓
evaluation of $f$ for a value outwith the range award 0.	min $4\frac{1}{4}$ , max $255\frac{7}{8}$	$\min 4\frac{1}{4}, \max 256\frac{1}{8}$
Candidate H	Candidate I	Candidate J
$f(x) = 4x^{-2} + x$	$f(x) = 4 + x^{3} \qquad \bullet^{1} \times$ $f'(x) = 0 + 3x^{2} = 0 \qquad \bullet^{2} \times$ $x = 0  f(x) = \text{undefine} \overset{3}{\overset{\checkmark}{\overset{\checkmark}{\overset{\checkmark}{}{\overset{\checkmark}{}{\overset{\checkmark}{}{\overset{\checkmark}{\overset{}{}{\overset$	$f'(x) = \frac{4}{2} + x = 0$ $\overset{\bullet^1 \times}{\overset{\circ}{}_{2}}$
$f'(x) = -8x^{-1}$	$f'(x) = 0 + 3x^2 = 0$ $e^2 \times e^3$	$x^2$ $x^3 \times$
$f'(x) = \dots + 1 = 0$	x = 0 $f(x) = $ undefined <sub>4</sub>	$f(1) = 5, f(4) = 4\frac{1}{4} \bullet^4 \times$
$\int (x) = \frac{1}{16} + 1 = 0$ $x = 8  f(x) = 8 \frac{1}{16}  \stackrel{\circ}{\bullet}^{2} \times \frac{1}{4 \sqrt{2}}$	• <sup>5</sup> ^	$4 \bullet 5 \checkmark \bullet 6 \land$
$f(1) = 5, f(4) = 4\frac{1}{4}$ $\overset{6}{\bullet}^{6}\sqrt{1}$		
min $4\frac{1}{4}$ , max $8\frac{1}{16}$		
Candidate K	Candidate L	Candidate M
	$f(x) = 4x^{-2} + x \qquad \bullet^1 \checkmark$	$4x^{-2} + x$ $\bullet^1 \checkmark$
$f'(x) = -4x^{-1} + \frac{x^2}{2} \qquad \stackrel{\bullet^2}{\bullet^3} \times $	$\int 4x^{-2} + x = -4x^{-1} + \frac{x^2}{2} = 0 \overset{\bullet^2}{\underset{\bullet^3}{\bullet^3}} \overset{\times}{\times}$	$-4x^{-1} + \frac{x^2}{2} = 0$ $\overset{\bullet^2}{\longrightarrow} \overset{\times}{} \overset{\bullet^3}{\times}$
$x = 2$ $f(2) = 3$ $4 \sqrt{1}$	$x = 2  f(2) = 3 \qquad \qquad \bullet^4 \times $	$x = 2$ $f(2) = 3$ $\bullet^4 \times$
$f(1) = 5, f(4) = 4\frac{1}{4}$ $6^{6}$	$\int 4x^{-2} + x = -4x^{-1} + \frac{x^2}{2} = 0 \stackrel{\circ}{\overset{\circ}{_3}} \times x = 2  f(2) = 3 \qquad \stackrel{\circ}{_4} \times f(1) = 5, \ f(4) = 4\frac{1}{4} \qquad \stackrel{\circ}{_6} \times f(4) \qquad \stackrel{\circ}{_6} \times f(4$	$f(1) = 5, f(4) = 4\frac{1}{4} = 6^{6} \times 6^{6}$
min 3, max 5	min 3, max 5	min 3, max 5

Question	Generic Scheme	Illustrative Scheme	Max Mark
23.			
• <sup>1</sup> collect log te	rms	Method 1	
		• $\log_2(3x+7) - \log_2(x-1) = 3$	
$a^2$ use lows of $b$		stated or implied by $\bullet^2$	
• <sup>2</sup> use laws of lo	JÄR N		
		• $\log_2 \frac{(3x+7)}{(x-1)} = 3$	
$\bullet^3$ use laws of lo	ogs		
		• $3\frac{(3x+7)}{(x-1)} = 2^{3}$	
• <sup>4</sup> solve for $x$		• $\frac{3}{(3x+7)} = 2^3$	
• solve for $x$		(x-1)	
		$\bullet^4 x = 3$	
		• $x = 3$	
		Method 2	
		• <sup>1</sup>	
		$\log_2(3x+7) = 3\log_2 2 + \log_2(x-1)$	
		stated or implied by $\bullet^2$	
		•2	
		$\log_2(3x+7) = \log_2 2^3 + \log_2(x-1)$	
		• $^{3} \log_{2}(3x+7) = \log_{2}8(x-1)$	
		$\log_2(3x+7) = \log_2 3(x-1)$	
		$\bullet^4 x = 3$	
			4
Notes:			
1. For $\bullet^3$ accept	$\log_2 \frac{(3x+7)}{(x-1)} = \log_2 8.$		
Commonly Observed	erved Responses:	Candidate B	
Candidate A			
$\log_2(3x+7) = 3 + 1$	$-\log_2(x-1)$	$\log_2(3x+7) = 3 + \log_2(x-1)$	
	$-\log_2(3x+7)$ $\bullet^1 \checkmark$	$\log_2(3x+7) + \log_2(x-1) = 3$	
		$\log_2(3x+7)(x-1) = 3 \qquad \bullet_2^1 \times$	
$-3 = \log_2 \frac{x-1}{3x+7}$	$\bullet^2 \checkmark$ $\bullet^3 \checkmark$	● <sup>2</sup> ✓	
	• <sup>4</sup> ✓		
$\frac{x-1}{3x+7} = 2^{-3}$	• •	$3x^2 + 4x - 15 = 0 \qquad \qquad \bullet^4 \checkmark$	
8x - 8 = 3x + 7		(3x-5)(x+3) = 0	
x = 3		$x = \frac{5}{3}$ or $x = -3$	
		$x = \frac{1}{3}$ of $x = -3$	ailable
		discard as $x > 1$ for candida	
		$x = \frac{5}{3}$ do not disc x = -3	
		I	

Question	Generic Scheme	Illustrative Scheme	Max Mark
24.			
• <sup>1</sup> interpret t substitute	he values of <i>a</i> , <i>b</i> and <i>c</i> and	• <sup>1</sup> $3^2 - 4 \times k \times 9k$	
• <sup>2</sup> know to use	discriminant $\geq 0$	$\bullet^2 \dots \ge 0$	
• <sup>3</sup> simplify or fa	<b>Method 1</b> actorise quadratic inequation	Method 1 • ${}^{3}$ $k^{2} \le \frac{9}{36}$ or $9(1-2k)(1+2k) \ge 0$	
• <sup>4</sup> state range c	of values of <i>k</i>	• $4 -\frac{1}{2} \le k \le \frac{1}{2}$ Method 2	
• <sup>3</sup> simplify or fa	Method 2 actorise quadratic expression	• <sup>3</sup> 9-36 $k^2 = 0 \Longrightarrow k = -\frac{1}{2}, \frac{1}{2}$	
• <sup>4</sup> evidence and	I range of values of <i>k</i>	• <sup>4</sup> graph or other evidence leading to $-\frac{1}{2} \le k \le \frac{1}{2}$	4
Notes:			<u> </u>
<ol> <li>The "≥0 "must appear at least once at the •<sup>1</sup> or •<sup>2</sup> stage for •<sup>2</sup> to be awarded.</li> <li>If an <i>x</i> appears in the candidate's 'discriminant' only •<sup>2</sup> may be awarded.</li> <li>The use of any expression masquerading as the discriminant can gain only •<sup>2</sup> at most.</li> <li>Award •<sup>2</sup> to candidates who write BOTH 9-36k<sup>2</sup> &gt; 0 AND 9-36k<sup>2</sup> = 0.</li> <li>For candidates who at •<sup>3</sup> simplify or factorise an equation •<sup>4</sup> can only be awarded if evidence of solving an inequation (for example a graph) appears.</li> <li>At •<sup>2</sup> stage, quoting b<sup>2</sup> - 4ac ≥ 0 is not sufficient.</li> <li>At •<sup>3</sup> stage, in Method 2, solutions for <i>k</i> need not be simplified.</li> </ol>			

Question	Generic Scheme	Illustrative Scheme	Max Mark
25(a)			
• <sup>1</sup> know to u distance for	ise Theorem of Pythagoras' or mula	• $D = \sqrt{(2t-5)^2 + (t-10)^2}$	
• <sup>2</sup> process to o	btain result	$D = \sqrt{4t^2 - 20t + 25 + t^2 - 20t + 100}$ $= \sqrt{5t^2 - 40t + 125}$	2
Notes:			<u> </u>
Be wary of fuc	lged solutions!		
Commonly Obs	served Responses:		
Candidate A		Beware	
$D = \sqrt{5t^2 - 40t} + $	$\frac{\overline{(0)^2 + (0 + (t - 10))^2}}{-125}  \bullet^2 \times$	$A(2t-5,0) \ B(0,t-10)$ $\overline{AB} = \begin{pmatrix} 0 \\ t-10 \end{pmatrix} - \begin{pmatrix} 2t-5 \\ 0 \end{pmatrix} = \begin{pmatrix} 2t-5 \\ t-10 \end{pmatrix} \bullet$ $D = \sqrt{(2t-5)^2 + (t-10)^2}$ $D = \sqrt{4t^2 + t^2 - 20t - 20t + 25 + 100}$	$2^{1} \times 1^{2}$
		$D = \sqrt{5t^2 - 40t + 125}$ NB: This is an exception to note general instructions	12 in the
25(b)			
• <sup>3</sup> write in diff	erentiable form	• ${}^{3}\left(5t^{2}-40t+125\right)^{\frac{1}{2}}$	
• <sup>4</sup> start differe	entiation	• $\frac{1}{2}(5t^2-40t+125)^{-\frac{1}{2}}$	
• <sup>5</sup> complete di	fferentiation	• <sup>5</sup> ×(10 <i>t</i> -40)	
• <sup>6</sup> substitute $t$	= 5 and interpret result	• <sup>6</sup> $D'(5) = \frac{10}{2\sqrt{50}} > 0$ increasing	4
Notes:			
2. Do not pena	Tailable for differentiating an expression expression $t$ and t	ession of the form (trinomial) <sup>proper fra</sup> te into a derivative.	ction

Commonly Observed Responses:	
Candidate A	Candidate B
$D(t) = (5t^{2} - 40t + 125)^{-1} \qquad \bullet^{3} \times \\ D'(t) = -(5t^{2} - 40t + 125)^{-2} \dots \qquad \bullet^{4} \times \text{ see note } 1. \\ \bullet^{5} \checkmark \\ = \dots \times (10t - 40) \qquad \bullet^{6} \checkmark 1$ $D'(5) = \frac{-10}{50^{2}} < 0 \therefore \text{ decreasing}$	$D(t) = (5t^{2} - 40t + 125)^{-\frac{1}{2}} \qquad \bullet^{3} \times D'(t) = -\frac{1}{2}(5t^{2} - 40t + 125)^{-\frac{3}{2}} \dots \qquad \bullet^{4} \checkmark 1$ =×(10t - 40) $D'(5) = \frac{-5}{\sqrt{50^{3}}} < 0 \therefore \text{ decreasing}$
Candidata C	<b>N</b> 30
Candidate C	Candidate D
$D(t) = (5t^{2} - 40t + 125)^{\frac{1}{2}} \qquad \bullet^{3} \checkmark \\ \bullet^{4} \times \\ D'(t) = \frac{1}{2} (5t^{2} - 40t + 125)^{\frac{3}{2}} \dots \\ \bullet^{5} \checkmark \\ \bullet^{6} \checkmark 1 \\ D'(5) = 5\sqrt{50^{3}} > 0 \therefore \text{ increasing}$	$D(t) = (5t^{2} - 40t + 125)^{\frac{1}{2}} \qquad $
Candidate E	Candidate F - Alternative Method
$D(t) = (5t^{2} - 40t + 125)^{\frac{1}{2}} \qquad \stackrel{\bullet^{3}}{\bullet^{4}} \checkmark \\ D'(t) = \frac{1}{2} (5t^{2} - 40t + 125)^{-\frac{1}{2}} \times 10t - 40 \qquad \stackrel{\bullet^{5}}{\bullet^{6}} \checkmark \\ D'(5) = \frac{1}{\sqrt{2}} > 0  \therefore \text{ increasing}$	$D^{2} = 5t^{2} - 40t + 125$ $\frac{dD^{2}}{dt} = 10t - 40$ $t = 5 \Rightarrow \frac{dD^{2}}{dt} = 50 - 40$ $\frac{dD^{2}}{dt} = 10 > 0  \therefore D^{2} \text{ is increasing}$ $D = 10 > 0  \therefore D^{2} \text{ is increasing}$
Calculating Distance	∴ D is increasing Alternative Response
t = 5 $D = \sqrt{50}$ t = 4 $D = \sqrt{45}$ so distance is increasing • <sup>6</sup> × Award 0 marks as answer is not from differentiation.	D <sup>2</sup> = 5(t <sup>2</sup> - 8t + 25) D <sup>2</sup> = 5[(t - 4) <sup>2</sup> + 9] Graph together with a statement indicating that when t = 5, D <sup>2</sup> is increasing and therefore D is increasing. $\overset{3}{} \checkmark$ $\overset{4}{} \checkmark$ $\overset{5}{} \checkmark$ $\overset{6}{} \checkmark$