



# SPTA

## Higher Homework

### Logs and Exponentials (B)



1. Simplify

(a)  $\log_5 125$       (b)  $\log_4 16 + \log_4 8 - \log_4 32$       (c)  $\frac{1}{3} \log_9 27$  (6)

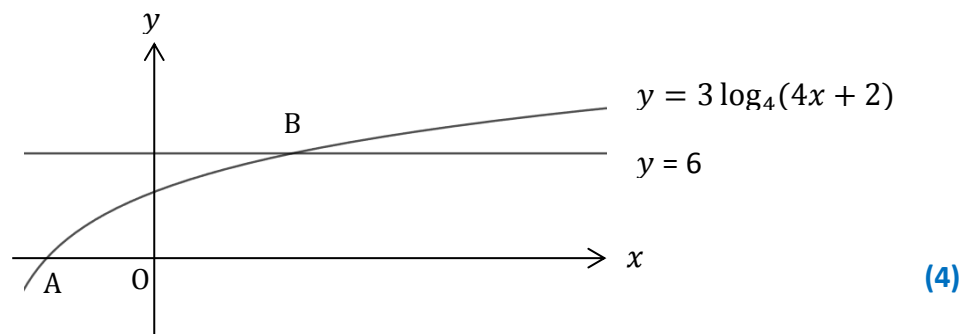
2. Solve the following for  $x$ ,  $x > 0$

(a)  $\log_5(x^2 - 1) - \log_5(x + 1) = 3$       (b)  $\log_3(x - 1) + \log_3(x + 1) = 1$  (6)

3. Part of the graph of  $y = 3 \log_4(4x + 2)$  is shown below.

The graph crosses the  $x$ -axis at the point A and the line  $y = 6$  at the point B.

Find the  $x$ -coordinate of B



4. The formula  $A = A_0 e^{-kt}$  gives the amount of a radioactive substance after a time  $t$  minutes. After 4 minutes 50g is reduced to 45g.

(a) Find the value of  $k$  to two significant figures (3)

(b) How long does it take for the substance to reduce to half its original weight? (3)

5. Two variables,  $x$  and  $y$ , are related by the equation  $y = kx^n$

When  $\log_5 y$  is plotted against  $\log_5 x$ , a straight line passing through the points A(0.5, 0) and B(0, 1) is obtained, as shown in the diagram.

Find the values of  $k$  and  $n$ .

